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Properties of Co-Mo coatings obtained by electrodeposition at pH 6.6

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Abstract Cobalt-molybdenum coatings were prepared by electrodeposition in a sulfate-citrate bath and their morphology, structure and magnetic properties were analysed. Concentrations of 0.1 mol dm^{-3} CoSO₄ and $0.005 \text{ mol dm}^{-3} \text{ Na}_2 \text{MoO}_4$ at pH 6.6 led to Co-Mo deposits of 20-23% Mo that can be grown to several microns over graphite or copper substrates. At low deposition potentials or current densities, the deposits presented a close-packed hexagonal structure (hcp) that evolved to a (100) + (110) preferred orientation and acicular morphology as the deposit thickness increased. When the deposition potential or the current density was made more negative, a mixed crystalline + amorphous structure was obtained. The degree of crystallinity depended on the thickness: thin films were more amorphous than the thicker ones. Co-Mo deposits showed lower saturation magnetization (M_s) and coercivity (H_c) than the pure cobalt deposits. The crystalline+amorphous films showed the lowest H_c values (around 40 Oe).

Keywords Cobalt-molybdenum alloy · Electrodeposition · Magnetic films · X-ray diffraction

Introduction

Magnetic materials of iron group metals have wide applications in industry, mainly in micro-electromechanical systems (MEMS) and magnetic storage devices.

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Serveis Cientificotècnics, Universitat de Barcelona, Lluis Solé i Sabaris 1–3, 08028 Barcelona, Spain The presence of molybdenum modifies their magnetic properties [1, 2] and improves their hardness and corrosion resistance [3, 4, 5]. These new properties make iron group metal-molybdenum alloys promising materials for microelectronic applications.

Interest in the electrodeposition of molybdenum with iron group metals has thus increased. Codeposition of molybdenum with iron group metals is induced, since complete reduction of molybdenum in aqueous solutions does not occur in the absence of an iron group metal [6]. Several studies have examined the anomalous electrodeposition of Ni-Mo [7, 8, 9, 10, 11, 12, 13, 14, 15], especially in a citrate medium, although there are fewer reports on Co-Mo or Fe-Co deposition [16, 17, 18].

In a previous study [2] the Co-Mo electrodeposition from a sulfate-citrate bath was explored. The percentage of Mo in the deposits was up to 60%, although the films were highly stressed. It was claimed that the presence of Mo led to soft magnetic behaviour.

A more recent study of the influence of bath composition and pH on the electrochemical behaviour of Co-Mo deposition suggested that the equilibria between the species in solution played an important role. It was found that alloy deposition occurred through different stages depending on the pH of the bath, which affected the composition of the final deposit [19]. We fixed the working pH at 6.6 to decrease simultaneous hydrogen evolution. In the present study, bath composition was fixed at 0.1 mol dm⁻³ cobalt sulfate and 0.005 mol dm⁻³ sodium molybdate. Citrate concentration was adjusted at 0.2 mol dm^{-3} in order to complex cobalt(II); higher citrate concentrations hinder the codeposition and decrease the efficiency of the process [19]. Molybdate concentration was kept low to prevent large Mo incorporation in the deposits, which would decrease the saturation magnetization of the coating.

The aim of the present study was to examine the influence of various electrodeposition parameters on the properties of the deposit at this fixed bath composition. We tested the deposition over a range of substrates in order to improve the film adherence and we analysed the influence of the thickness and the electrodeposition conditions on structure and magnetic properties, since our main interest was the preparation of homogeneous films with soft magnetic behaviour.

Experimental

The electrochemical measurements were performed in a conventional three-electrode cell using a microcomputer-controlled Autolab potentiostat/galvanostat with PGSTAT30 equipment and GPES software. All chemicals used were of analytical grade. Solutions were freshly prepared with water that was first doubly distilled and then treated with a Millipore Milli-Q system. Before and during the experiments, solutions were de-aerated with argon. The temperature was maintained at 25 °C.

The morphology of the deposits was examined with a Hitachi S 2300 scanning electron microscope. Elemental composition was determined with an X-ray analyser incorporated in a Leica Cambridge Stereoscan S-360 scanning electron microscope. The efficiency of deposition was calculated by comparing the reduction charge and the results of chemical analysis of the films. For chemical analysis, the deposits were dissolved in 5 mL of 1% nitric acid solution and samples were analysed by inductively coupled plasma mass spectrometry (ICP-MS). Measurements were made in a Perkin-Elmer spectrometer Elan 6000. Certified standard solutions of cobalt and molybdate ions containing rhodium as an internal standard were used to calibrate the instrument.

The thickness of the deposits was measured on a Zeiss Axiovert 405M microscope.

X-ray diffraction (XRD) phase analysis was performed in a Philips MRD diffractometer in low-resolution parallel beam optics. The Cu-K_x radiation ($\lambda = 1.5418$ Å) was selected by means of a diffracted-beam flat graphite monochromator. Diffractograms were obtained in the 20–100° 2 θ range with a step of 0.05° and a measuring time of 5″ per step. The magnetic measurements were performed with a Manics DSM8 pendulum-type magnetometer at room temperature or with a SQUID magnetometer.

Vitreous carbon (r = 1.0 mm), graphite (r = 4.1 mm) and copper (r = 1.0 mm) rods were used as working electrodes. The vitreous carbon electrode was polished to a mirror finish before each experiment using alumina of different grades (3.75 and 1.85 µm) and cleaned ultrasonically for 2 min in water. Copper and graphite electrodes were also polished before each experiment using sandpaper (2400 and 4000) and, later, damp alumina (0.3 µm). The reference electrode was an Ag/AgCl/1 mol dm⁻³ NaCl electrode mounted in a Luggin capillary containing 0.5 mol dm⁻³ Na₂SO₄ solution. All potentials are referred to this electrode. The counter electrode was a platinum spiral.

During electrodeposition the solution was gently stirred ($\omega = 60$ rpm) to avoid the depletion of the minority species (molybdate) to the electrode and to ensure homogeneous composition of the deposits.

Results and discussion

Electrochemical study

The general behaviour of Co-Mo deposition was analysed on vitreous carbon, graphite and copper substrates to identify the best electrode for thick-adherent coatings. Voltammetric, chronoamperometric and chronopotentiometric studies were carried out for this purpose.

The redox process was similar in all substrates, but the electrodes behaved differently in the reduction (Fig. 1). Copper was the most active substrate and



Fig. 1 Cyclic voltammograms of a 0.1 mol dm⁻³ CoSO₄+0.2 mol dm⁻³ Na₃C₆H₅O₇+0.005 mol dm⁻³ Na₂MoO₄, pH 6.6, solution (Co-Mo solution): (*a*) copper, (*b*) graphite and (*c*) vitreous carbon electrodes; scan rate 50 mV s⁻¹

vitreous carbon was the slowest. Alloy deposition started at around -900 mV for copper, at -1050 mV for graphite and at -1150 mV for the vitreous carbon electrode. A complex oxidation peak was observed in all cases, at around -200 mV. According to this, it seemed that alloy deposits could be obtained in a similar way over the different substrates, although the potential necessary to start the deposition process was different for each electrode.

To test the adherence of Co-Mo deposits on those substrates, various samples were prepared at long deposition times. When deposits were obtained potentiostatically on the vitreous carbon electrode, there were deformations in the j-t curves in spite of stirring (Fig. 2A) and the films were cracked (Fig. 2B). At longer deposition times the deposits fell off the substrate (Fig. 2C). Vitreous carbon was therefore ruled out. Graphite or copper substrates were suitable because the deposits did not detach even for thick coatings.

Characterization of the cobalt-molybdenum deposits

According to the results earlier obtained, Co-Mo deposits of several microns were prepared on graphite or copper electrodes. Morphological, compositional and structural characterization was carried out for each sample. Our main objective was focused on controlling the structure of the deposits, because it is known that structure and magnetic properties are usually related. Graphite electrodes were more useful because their greater area improved the resolution of the response.

Pure cobalt deposits were prepared from a molybdate-free bath in order to compare them with the Co-Mo



Fig. 2 A j-t transient from -500 mV to -980 mV; 60 rpm, vitreous carbon electrode, Co-Mo solution. B, C SEM images of the deposits obtained at points *a* and *b* of A, respectively

deposits. Potentials or current densities were chosen to give similar deposition rates.

Figure 3 shows the diffractograms of cobalt and cobalt-molybdenum (~23% Mo) deposits obtained at a similar deposition rate (j = -3.2 mA cm⁻²) and the corresponding chronopotentiometric curves. The potential



Fig. 3 A *E*–*t* transients recorded applying -3.2 mA cm⁻², graphite electrode, 60 rpm: (*a*) cobalt deposit obtained from a 0.1 mol dm⁻³ CoSO₄+0.2 mol dm⁻³ Na₃C₆H₅O₇, pH 6.6, solution; (*b*) Co-Mo deposit of 23% Mo obtained from the Co-Mo solution. **B** X-ray diffractograms of the deposits from **A**; 140 C cm⁻², 32 µm

related to pure cobalt deposition evolved to a more negative value than that corresponding to Co-Mo deposition (Fig. 3A), because alloy deposition was favoured [2]. The diffractograms showed narrow peaks, revealing the crystalline nature of the deposits (Fig. 3B). For pure cobalt, the main peaks corresponded to a closepacked hexagonal structure (hcp), whereas a small peak around $2\theta = 51.5^{\circ}$ is attributed to face-centred cubic (fcc) cobalt deposited next to the main hcp structure.

The diffractogram of a Co-Mo deposit shows a pure hcp structure, although the position and relative height of the peaks are different from the pure cobalt deposit. The peaks of the hexagonal structure were shifted to lower values corresponding to an increase of the cell parameters, as a consequence of the incorporation of molybdenum. The cell parameters of this hexagonal structure were calculated after fit profile and least-squares refinement, leading to values of a=2.550 Å and c=4.125 Å, greater than those for pure cobalt (a=2.507 Å, c=4.092 Å). Moreover, the Co-Mo deposit showed greater orientation, the *hk*0 being the main diffraction peaks. The practical absence

of peaks with $l \neq 0$ indicated that the [001] crystallographic direction was nearly parallel to the substrate surface.

In a previous study, thinner $(0.2 \ \mu\text{m})$ Co-Mo deposits with an amorphous structure had been obtained [2]. In contrast, Co-Mo deposits of several microns prepared in the present work had a crystalline structure. Since the former were prepared potentiostatically and using a vitreous carbon electrode, we explored the influence of deposition parameters on the structure of the Co-Mo coatings.

Influence of deposition technique and the substrate nature

For all the conditions tested, potentiostatic and galvanostatic techniques led to equivalent electrochemical parameters: when a current density value j_1 was applied, the potential reached a stationary value E_1 ; analogously, when E_1 was the potential value applied, the stationary current recorded from the j-t transient was j_1 . Moreover, by comparing the deposits obtained with both techniques, the same morphology and composition were found.

For example, irrespective of the technique, thick Co-Mo deposits corresponded to an acicular morphology when a graphite substrate was used (Fig. 4). The process was highly efficient for these deposits (around 85%).

On the other hand, the galvanostatic transients of Co-Mo deposition over graphite and copper electrodes at the same current density $(-3.2 \text{ mA cm}^{-2})$ showed that practically the same stabilization potential was attained in both cases. The deposits obtained on copper substrate at long deposition times showed the same morphology and composition as those obtained over the graphite electrode.

When the diffractograms of the thick Co-Mo deposits obtained through the potentiostatic/galvanostatic technique and over the copper/graphite substrate were compared, similar profiles were also observed (Fig. 5). An hcp structure with hk0 main peaks was always obtained. The position of these peaks did not change, as corresponds to a given value of the molybdenum percentage. Similar results were obtained when potentials lower than -1000 mV were used.

Influence of the deposit thickness

When deposits obtained at different deposition times for a given potential value were analysed, it was corroborated that the composition of the coatings did not change with the deposition time, due to the stirring conditions. However, the morphology and structure presented some differences as a function of the reduction charge. Thick Co-Mo coatings had the morphology shown in Fig. 4, while thinner coatings presented the morphology shown in Fig. 6A. Figure 6B shows the corresponding X-ray diffractograms. A relationship between the change in the morphology and the structure was observed. As the thickness of the deposit increased, the hcp structure increased its preferred orientation, leading to a structure with a clear (100) + (110) preferred orientation. At the same time, the morphology changed from a polyhedral grain to acicular.

Influence of the deposition potential

The influence of the deposition rate on the morphology and structure of the coatings was analysed by means of the variation of the deposition potential, because the deposition rate increases as the applied potential is more



Fig. 4 SEM image of a deposit obtained at -940 mV during 55,000 s; 23% Mo, 32 μ m, Co-Mo solution, 60 rpm, graphite electrode



Fig. 5 X-ray diffractograms of the deposits obtained at -3.2 mA cm^{-2} from the Co-Mo solution; 60 rpm: (*a*) copper electrode, (*b*) graphite electrode





Fig. 6 A SEM micrograph of the deposits obtained at -940 mV from the Co-Mo solution; 60 rpm, graphite electrode, 8 μ m. **B** X-ray diffractograms of Co-Mo deposits with (*a*) 8 μ m and (*b*) 32 μ m

negative. In the potential range studied, the applied potential had little effect on the composition (Table 1). However, a clear decrease of the deposit thickness was obtained by making more negative the deposition potential as a consequence of the lowering of the efficiency (η) .

The morphology, composition and crystalline structure of the deposits obtained at a fixed charge (20 C cm^{-2}) were studied. Deformations in the *j*-*t* transients were observed for potentials equal to or more negative than -1000 mV (Fig. 7A), probably attributable to simultaneous hydrogen evolution. At deposition potentials less negative than -1000 mV, non-cracked coatings were obtained (Fig. 7B, image a), showing the previously described polyhedral morphology for thin Co-Mo films. In contrast, stressed and cracked deposits were obtained from -1000 mV (Fig. 7B, images b and c). Diffractograms of deposits obtained at different potentials showed some differences, as can be observed in the magnified X-ray diffractograms in the range 35– $60^{\circ} 2\theta$ (Fig. 7C). For the deposits obtained at -940 mV,

 Table 1 Molybdenum percentages in Co-Mo coatings obtained at different deposition potentials

-E (mV)	% Mo	η (%)
930	21	85
940	23	88
970	20	75
1000	22	53
1100	23	13
1200	22	6

the narrow 100, 002 and 101 peaks of the hexagonal structure can be observed next to small peaks of the substrate. For those obtained at -1000 mV, there were small 100 and 101 peaks corresponding to a hexagonal crystalline structure, peaks corresponding to a graphite substrate and a very wide peak $(3.5^{\circ} 2\theta)$ centred on 44.5° 2θ and attributed to an amorphous Co-Mo phase [2]. Thus, at this potential, the deposit seems to have a mixed crystalline and amorphous structure. The diffractogram of the deposit obtained at -1100 mV mainly showed peaks of the substrate and a wide peak attributed to the amorphous phase. Thus, a decrease of the deposition potential, i.e. an increase of the deposition rate, favoured the formation of less crystalline deposits. For the crystalline + amorphous samples, the presence of cracks or a non-compact structure allowed the observation of the substrate peaks in the diffractogram.

At higher deposition charges of around 150 C cm⁻², for which deposits of several microns were obtained, XRD revealed the formation of crystalline deposits at -940 and -1000 mV. On the other hand, a mixture of crystalline + amorphous phases was detected at -1100 mV, since the 100 peak of the hcp structure and the wide peak attributed to the amorphous structure were detected (Fig. 8). This result evidenced that, at the intermediate deposition potential (-1000 mV), the crystallinity increased with the deposit thickness. In contrast, for the deposits prepared at E < -1000 mV, the structure was not affected by the deposit thickness.

Magnetic behaviour of Co-Mo films

Since different Co-Mo structures were observed as a function of the deposition potential (or current density), deposits of several microns were prepared to analyse their magnetic properties. A graphite electrode and high thicknesses were selected to facilitate separation of the coatings from the substrate.

The magnetic properties were determined by recording hysteresis loops (Fig. 9). The easy axis is the in-plane direction of the parallel film. For a parallel applied field (H_{\parallel}) a large saturation field $(H_{s\parallel})$ of about 9 kOe was required to align the magnetization in the film plane and a low remanence value was observed. The results obtained under a perpendicular field (H_{\perp}) were similar, except that the saturation field $(H_{s\perp})$ was about 20 kOe. These features indicated strong uniaxial

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Fig. 7 A *j*-*t* transients of the Co-Mo solution; 60 rpm, graphite electrode: (*a*) -940, (*b*) -1000, (*c*) -1100 mV. **B** SEM images of the deposits obtained from **A**; 20–23% Mo, 20 C cm⁻²: (*a*) 4.6 μ m, (*b*) 2.7 μ m, (*c*) 0.8 μ m. **C** X-ray diffractograms of these deposits

anisotropy, in addition to the usual shape anisotropy [20].

The value of the uniaxial anisotropy constant (*K*) and the angle θ of the resulting anisotropy with respect to the film normal may be found using the expressions [21]:

$$H_{\rm S\parallel} = 2K\cos^2\theta/M_{\rm S} \tag{1}$$

and:

$$H_{\mathrm{S}\parallel} + H_{\mathrm{S}\perp} = 4\pi M_{\mathrm{S}} + 2K/M_{\mathrm{S}} \tag{2}$$

where M_s is the saturation magnetization. Values of $K\approx 6.4\times 10^6$ erg cm⁻³ and $\theta = 55^\circ$ were found.

A strong uniaxial anisotropy was observed for the Co-Mo samples, as expected for an hcp structure and



Fig. 8 X-ray diffractograms of deposits obtained under the same conditions as in Fig. 7 but with a greater charge: (a) -940, (b) -1000, (c) -1100 mV; 150 C cm⁻²; (a) 35 μ m, (b) 20 μ m, (c) 6.5 μ m



Fig. 9 Parallel and perpendicular hysteresis loops for a deposit obtained from Co-Mo solution; 60 rpm, graphite electrode, -3.2 mA cm^{-2} , 22% Mo, 40 μ m



Fig. 10 Magnetization versus magnetic field applied for the deposits obtained at 60 rpm over a graphite electrode: (*a*) 0.1 mol dm⁻³ CoSO₄+0.2 mol dm⁻³ Na₃C₆H₅O₇, pH 6.6 solution, -1120 mV, 37 µm; (*b*) Co-Mo solution, -940 mV, 35 µm; (*c*) Co-Mo solution, -1100 mV, 6.5 µm

high textured films. However, the *K* value obtained was greater than that corresponding to pure hcp cobalt $(K=4.5\times10^6 \text{ emu cm}^{-3})$ [20], probably due to the residual stress and distortions caused by the presence of molybdenum in the crystalline lattice of cobalt.

The magnetization curves of Co-Mo deposits were compared with those corresponding to pure cobalt deposits obtained from a molybdate-free solution and prepared at similar deposition rates (Fig. 10). For the pure cobalt coating with an hcp structure, a saturation magnetization of 135 emu g⁻¹ was obtained, which corresponded to a bulk cobalt response. The coercivity value (H_c) was around 160 Oe.

For cobalt-molybdenum deposits, a clear decrease of the saturation magnetization was observed, around 65 emu g^{-1} . This value was approximately constant for deposits prepared at different deposition rates, because they contained similar molybdenum percentages.

Moreover, the introduction of molybdenum in the deposits caused a clear decrease of the coercivity of the coatings. The Co-Mo films were soft, with coercivities in the range 70–40 Oe. The deposits obtained at potentials

no more negative than -1000 mV (or at current densities no more negative than -5 mA cm^{-2}) showed similar values of coercivity (around 70 Oe). However, deposits prepared at more negative values of the current density or the potential (until -1200 mV) showed a lower coercivity (around 40 Oe), revealing that amorphous + crystalline coatings presented the lowest value of any of these films.

Conclusions

Electrodeposition is a suitable way to obtain Co-Mo magnetic deposits over different substrates from a sulfate-citrate bath at pH 6.6. As deduced from voltammetric experiments, the start of the alloy deposition over vitreous carbon is delayed with respect to graphite and copper electrodes. Copper and graphite are useful to prepare Co-Mo coatings of several microns, whereas vitreous carbon favours detachment of the films.

The bath used, although it contains a low concentration of molybdate, leads to cobalt-molybdenum deposits of 20-23% Mo. This percentage is slightly dependent on the deposition potential or the current density applied. It is possible to maintain a constant composition through the thickness of the coating using moderate stirring of the solution during the deposition. No influence of the substrate (copper/graphite) or the preparation technique has been detected on the properties of the Co-Mo films. Co-Mo coatings of an hcp structure have been always obtained, and the cell parameters are clearly greater than those for the hexagonal cobalt. The films evolve with thickness to a structure with a clear (100) + (110) preferred orientation, showing an acicular morphology.

However, the properties (morphology, structure and magnetic properties) of the cobalt-molybdenum coatings are dependent on the deposition rate. The incorporation of molybdenum in the cobalt coatings leads to a decrease of both saturation magnetization and coercivity, with respect to the values for pure cobalt. The value of the saturation magnetization was constant for a fixed molybdenum percentage, but the value of the coercivity was also dependent on the crystalline structure of the films. Low deposition rates (low deposition potentials or current densities) favoured the formation of homogeneous crystalline deposits with a coercivity approximately constant. However, when high deposition rates were used to prepare the films, cracked coatings were obtained, with a mixed crystalline + amorphous structure and a lower coercivity than those for pure crystalline ones.

For the solution studied, the selection of both coating thickness and deposition potential (or current density) allows us to control the crystalline nature of the Co-Mo deposits. A decrease of the crystallinity improves the soft magnetic behaviour of the Co-Mo coatings.

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